

Inductors

Session 2b of “Basic Electricity”
A Fairfield University E-Course
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Basic Electricity

Two Sections

- Electron Flow and Resistance
 - 5 on-line sessions
 - Lab
- Inductance and Capacitance
 - 5 on-line sessions
 - Lab

Mastery Test, Part 1

Basic Electricity (Continued)

- **Text:** “Electricity One-Seven,” Harry Mileaf, Prentice-Hall, 1996, ISBN 0-13-889585-6 (Covers several Modules and more)
- **References:**
 - “Digital Mini Test: Principles of Electricity Lessons One and Two,” SNET Home Study Coordinator, (203) 771-5400
 - [Electronics Tutorial](#) (Thanks to Alex Pounds)
 - [Electronics Tutorial](#) (Thanks to Mark Sokos)
 - [Basic Math Tutorial](#) (Thanks to George Mason University)
 - [Vector Math Tutorial](#) (Thanks to California Polytec at atom.physics.calpoly.edu)

Section 2:

AC, Inductors and Capacitors

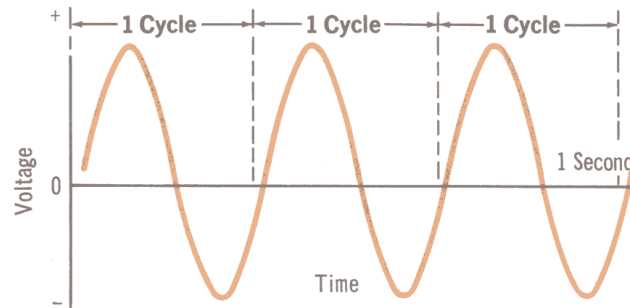
- **OBJECTIVES:** This section introduces AC voltage / current and additional circuit components (inductors, transformers and capacitors).

Section 2 Schedule:

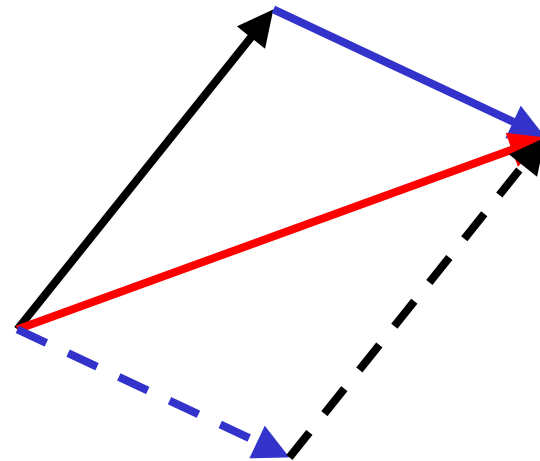
Session 2a	– 03/27	Alternating Current & Sine Waves	Text 3.1 – 3.41
Vector Math	– 04/01	Sine Waves, Magnitude, Phase and Vectors	Text 4.1 – 4.24
Session 2b (fri. review session?)	– 04/03	Inductors and Circuits	Text 3.42 – 3.73
Session 2c	– 04/08	Transformers	Text 3.74 – 3.100
Session 2d (lab - 04/13, Sat.)	– 04/10	Capacitors	Text 3.101 – 3.135
Session 2e	– 04/15	More Capacitors	Text 3.135 – 3.148
Session 2f	– 04/22	Review (Discuss Quiz_2)	

Vector Session Review

- Sine waves – $\sin(2\pi ft + \theta)$
 - Frequency (f)
 - Period & Wavelength (λ)
 - Amplitude (A)
 - Phase (θ)
 - Sin and Cos
 - Adding sine waves
- Vector analogy
 - Magnitude and Angle
 - Addition
 - Head-to-Tail
 - Parallelogram
 - Components (Later)

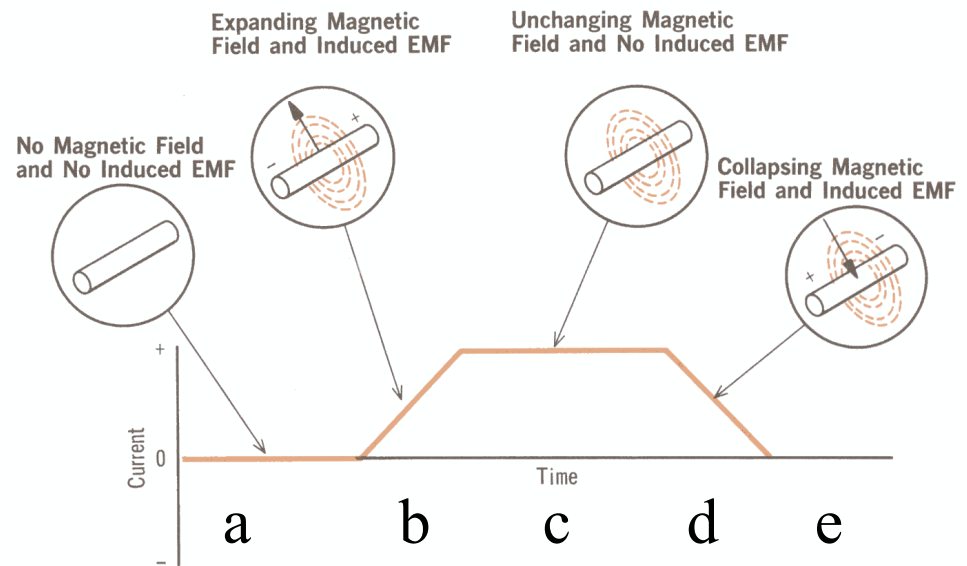


The frequency of a voltage or current is the number of cycles generated each second. The frequency of this voltage is, therefore, 3 Hz



EMF and Current

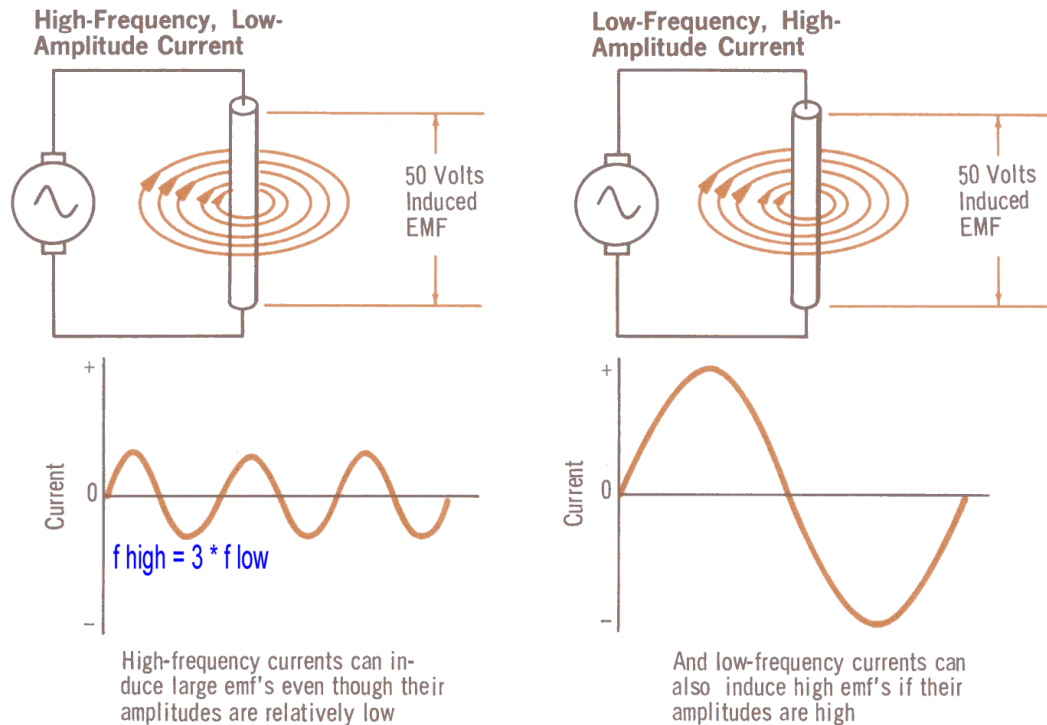
- a. No applied voltage;
no current
- b. Constant applied voltage;
linearly increasing current
- c. Zero applied voltage;
unchanging current
- d. Negative applied voltage;
linearly decreasing current
- e. no applied voltage;
no current



Frequency Effects

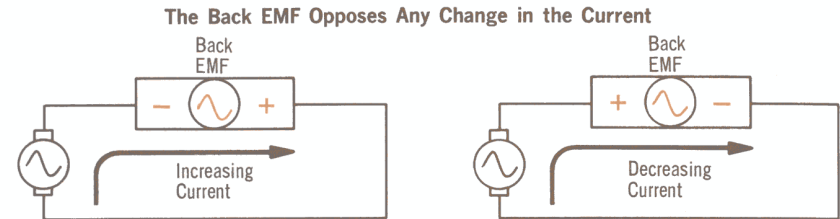
- To get the same effect from low frequency AC current, you need a higher current

The frequency of an a-c current and its amplitude determine the magnitude of the self-induced emf

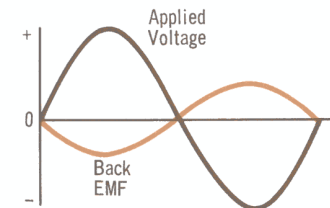


EMF Polarity vs. Applied Voltage

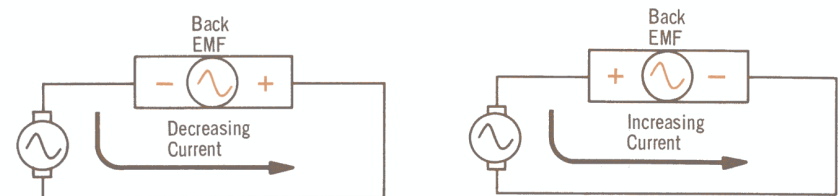
- Induced EMF always opposes voltage applied across the inductor



The polarity of the back emf is opposite to the circuit current when current is increasing, and the same as the circuit current when current is decreasing

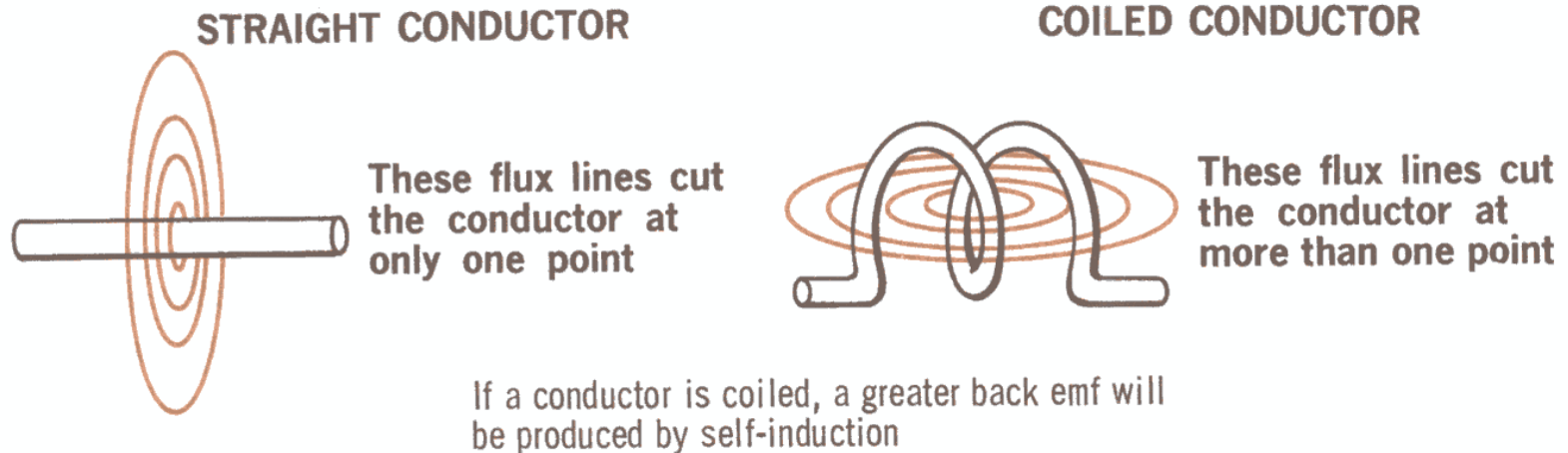


The back emf always opposes the applied voltage. Back emf is also known as counter emf or cemf



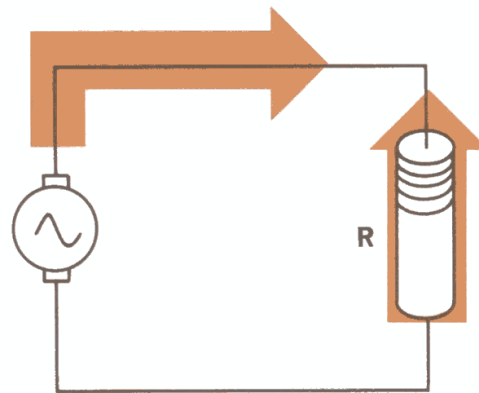
Coiling to Increase Inductance

- Coiling a wire increases its inductance
- Magnetic fields from each loop support each other (“mutual inductance”)

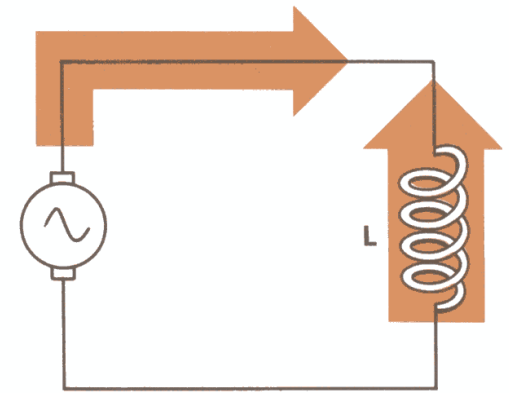


Resistors vs. Inductors

- Analogy to Ohm's law for resistors
- Inductors resist changes in their current with their "Reactance"

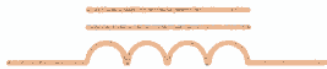
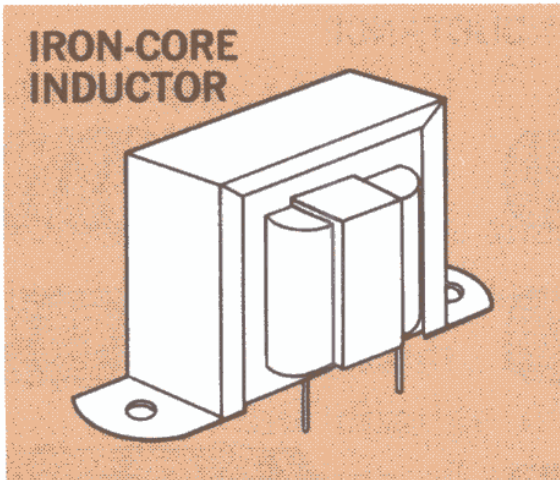


Resistors oppose all current in a circuit. They have resistance, which is abbreviated R

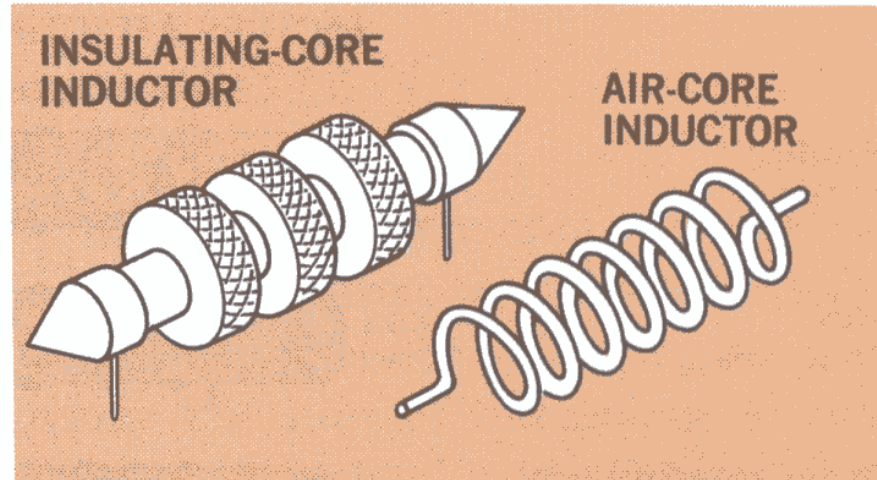


Inductors oppose changes in current in a circuit. They have inductance, which is abbreviated L

Real Inductors



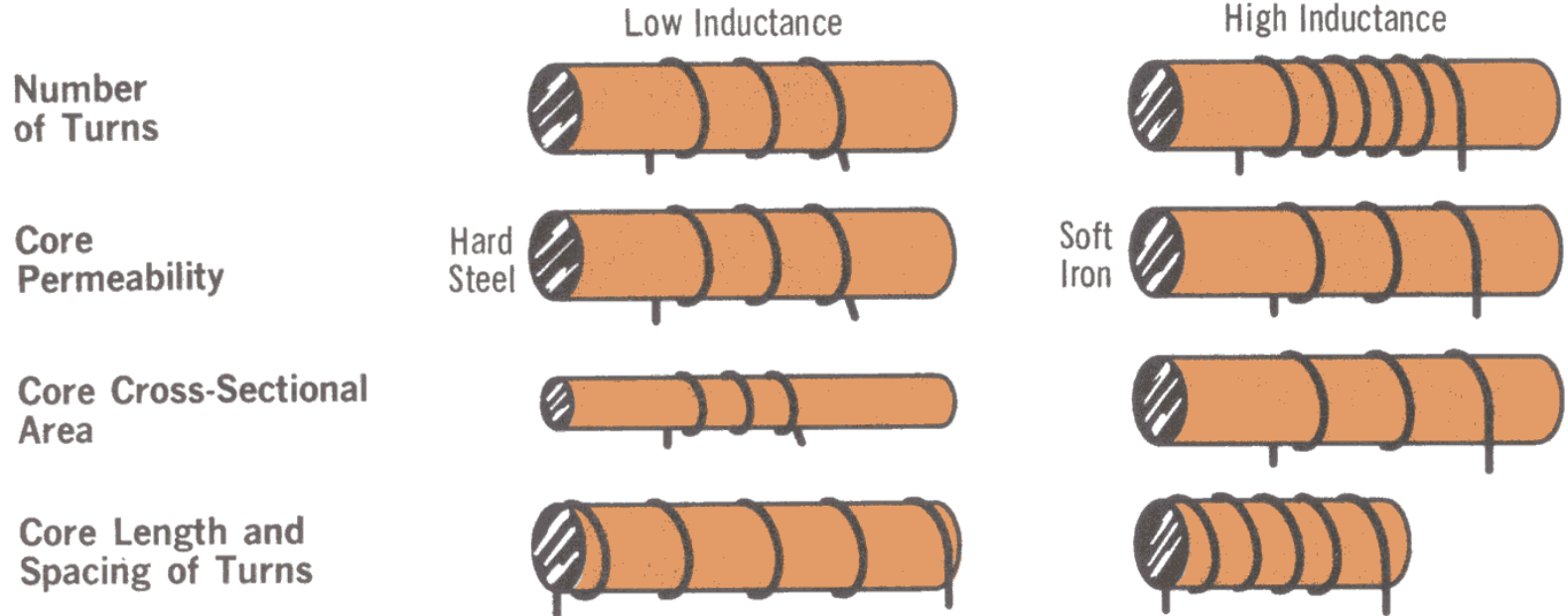
This is the symbol for an iron-core inductor



This is the symbol for an insulating-core inductor or an air-core inductor

Factors Affecting Inductance

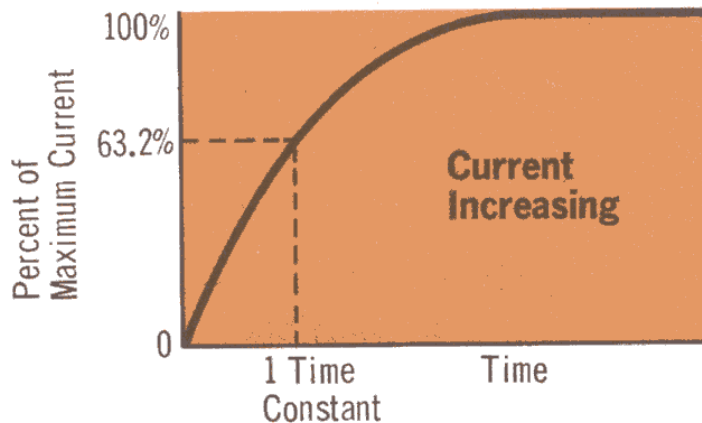
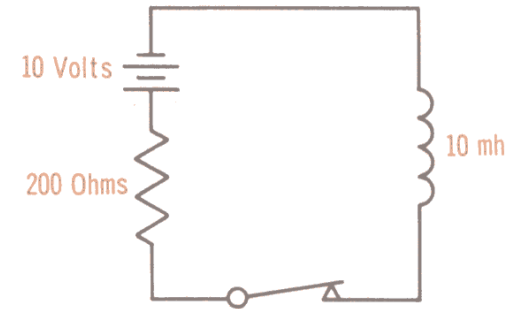
FACTORS AFFECTING INDUCTANCE



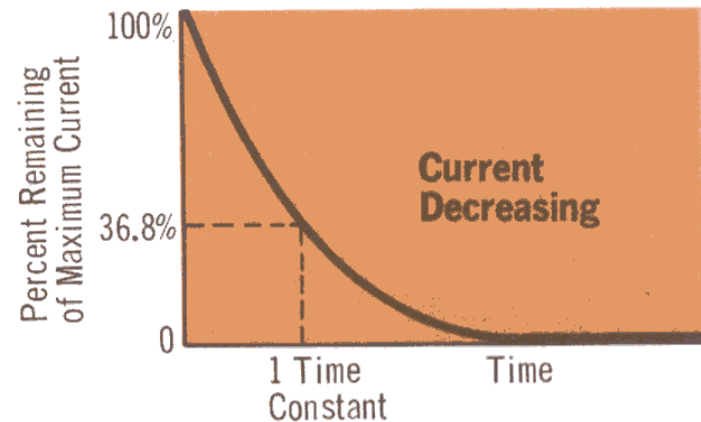
High inductance is obtained with a reasonably small inductor by winding the wire around the core in many layers

Inductor “Transient” Current

- DC applied to a series resistor and inductor circuit
- At $t=0$ inductor has a high “reactance” so no current
- After a while the inductor behaves like a short circuit
- The current rises “exponentially from 0 to V/R ”
- If the battery then drops to zero the reverse happens



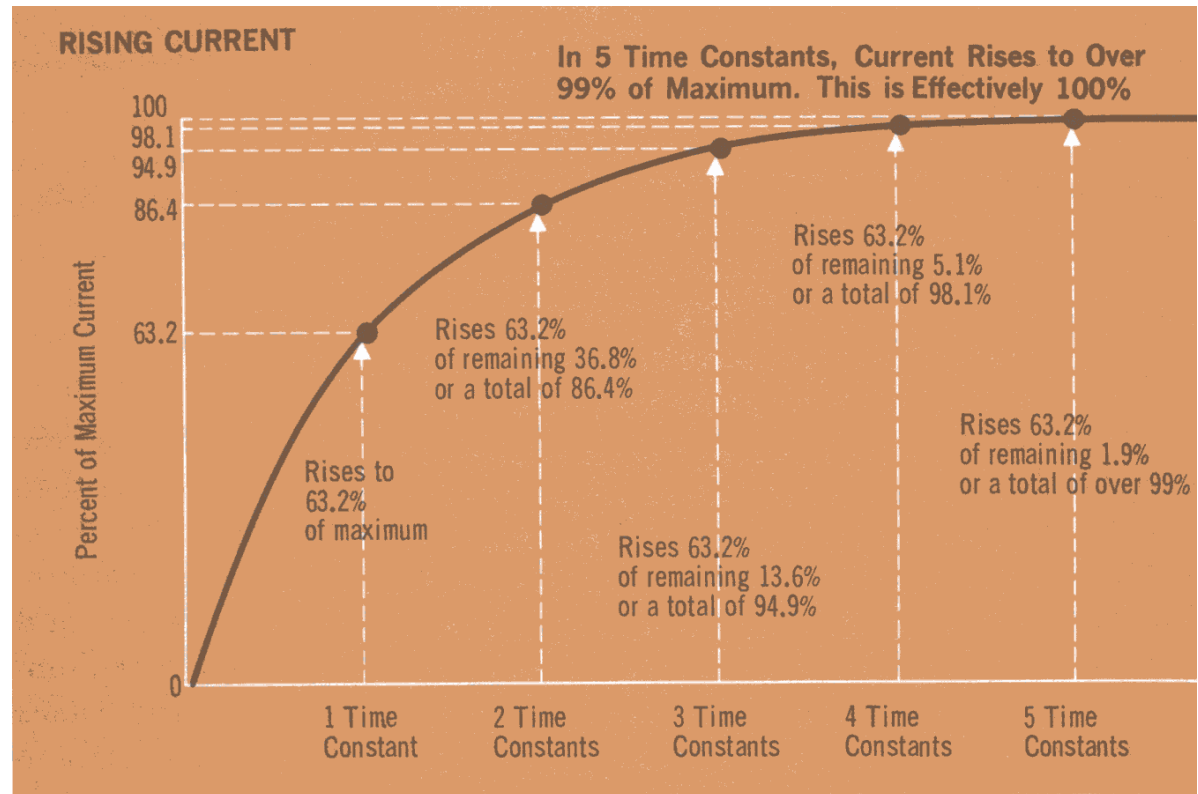
In 1 time constant the current increases from zero to 63.2% of its maximum value



In 1 time constant the current falls 63.2% from its maximum value, leaving 36.8%

Time Constant

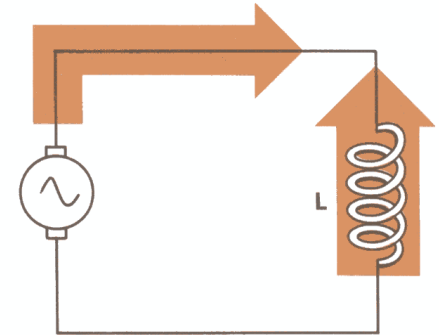
- Time constant
 $\tau = L/R$
- Formula
 $I = 1 - \epsilon^{-(t/\tau)}$
 $\epsilon = 2.7818$
(base of the natural logarithm)



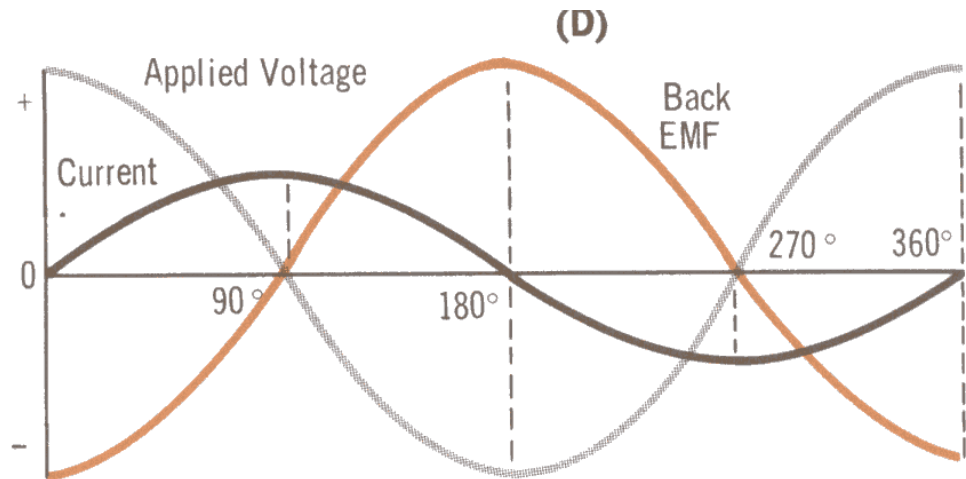
In each time constant, the current increases to a value 63.2% closer to its maximum value

AC Voltage and Current

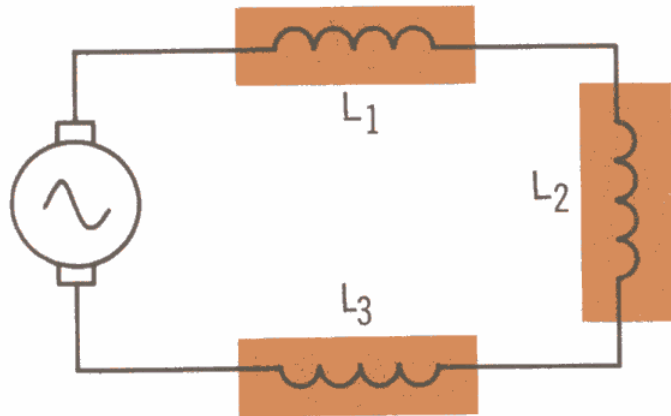
- Induced EMF “opposes” applied voltage
- Inductor current “lags” the voltage 90° (Eli the ice man)
- Inductor Reactance ($X_L = 2\pi fL$) determines the current magnitude ($|I| = |V| / X_L$)



In an inductance: (1) the applied voltage leads the current by 90° ; (2) the back emf lags the current by 90° ; and (3) the applied voltage and the back emf are 180° out of phase



Series and Parallel Inductors



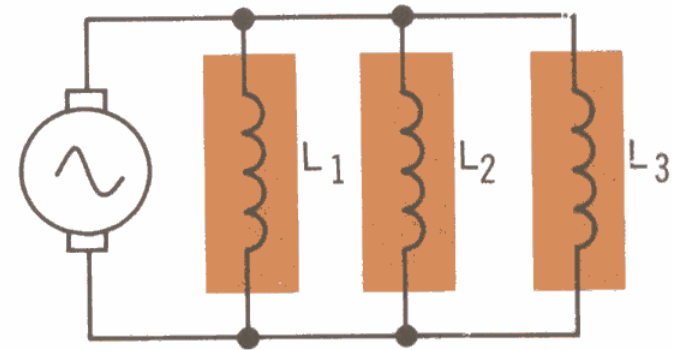
Total Inductance:

$$L_{TOT} = L_1 + L_2 + L_3$$

Total Inductive Reactance:

$$X_{L\ TOT} = X_{L1} + X_{L2} + X_{L3}$$

The total inductance or inductive reactance of series and parallel inductors is calculated the same as the total resistance of series and parallel resistance combinations



Total Inductance:

$$L_{TOT} = \frac{1}{\frac{1}{L_1} + \frac{1}{L_2} + \frac{1}{L_3}}$$

Total Inductive Reactance:

$$X_{L\ TOT} = \frac{1}{\frac{1}{X_{L1}} + \frac{1}{X_{L2}} + \frac{1}{X_{L3}}}$$

“Q”

- Quality factor “Q” of a coil is defined as the energy stored divided by the energy lost
 - Wire resistance
 - Losses in the “core”
- Calculating Q of an Inductor

$$Q = X_L / R_{\text{eff}}$$

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