

14.22 Find $v_o(t)$, for $t > 0$, in the network in Fig. P14.22 using Thévenin's theorem.

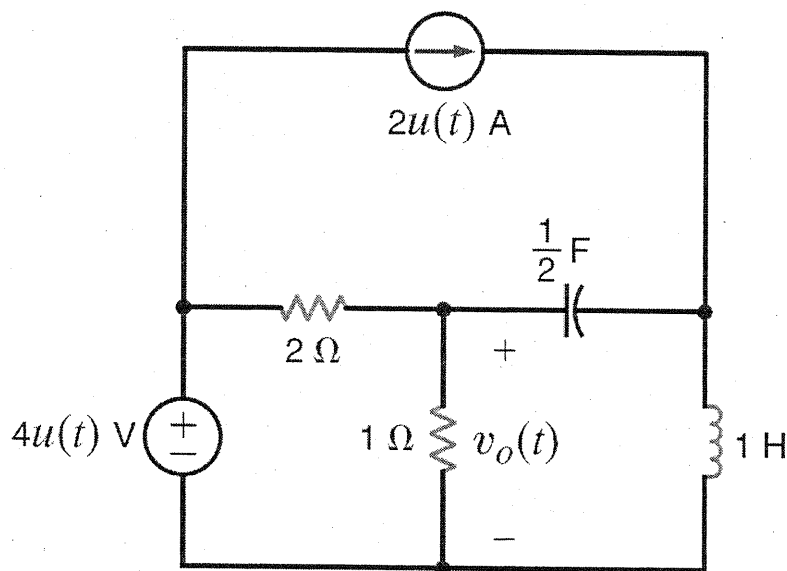
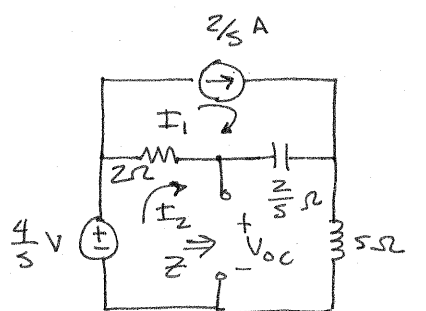
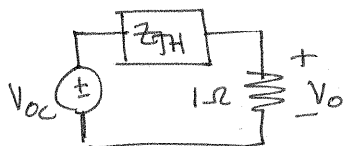


Figure P14.22

SOLUTION:



$$Z = \frac{Z \left(s + \frac{2}{s} \right)}{2 + s + \frac{2}{s}} = \frac{2s^2 + 4}{s^2 + 2s + 2}$$



$$I_1 = \frac{2}{s} \text{ A} \quad \frac{4}{s} = I_2 \left[2 + \frac{2}{s} + s \right] - I_1 \left[2 + \frac{2}{s} \right]$$

$$\text{or, } \frac{4}{s} = I_2 \left(\frac{s^2 + 2s + 2}{s} \right) - \frac{2}{s} \left(\frac{2s + 2}{s} \right)$$

$$I_2 = \frac{8s + 4}{s(s^2 + 2s + 2)}$$

$$V_{OC} = \frac{4}{s} - 2(I_2 - I_1) = \frac{8s^2 + 8}{s(s^2 + 2s + 2)}$$

$$V_O = \frac{V_{OC}(1)}{1 + Z_{TH}} = \frac{(8/3)(s^2 + 1)}{s(s^2 + \frac{2}{3}s + 2)}$$

$$V_O = \frac{4/3}{s} + \frac{K_1}{s + \frac{1}{3} - j\frac{\sqrt{17}}{3}} + \frac{K_1^*}{s + \frac{1}{3} + j\frac{\sqrt{17}}{3}}$$

$$K_1 = 0.825 \angle 36.0^\circ$$

$$v_o(t) = \left[\frac{4}{3} + 1.65 e^{-t/3} \cos\left(\frac{\sqrt{17}}{3}t + 36^\circ\right) \right] u(t) \text{ V}$$